Shadows
Terminology
Occluders: cast shadows
Receivers: have shadows on them
Point light sources: make hard shadows
Area light sources: make soft shadows
Umbra: the fully shadowed region
Penumbra: the partially shadowed region
Problem
Existing APIs do not completely solve the rendering equation - and do not include shadows
Solutions
Projection shadows
Idea: just project the occluder onto a receiving plane
How
One can derive the needed projection matrix Then apply the projection matrix to the occlude geometry

## Caveats

How to put the result on the receiving plane without being inside it (depth aliasing)?

Best solution: render receiving normally and first, then render the projected
occlude with z-buffering off, then render the rest of the scene normally What happens when the projected shadow falls outside the bounds of the receiver?

Solution: turn on the stencil buffer when rendering the receiver, use it when rendering the occluder

Note that this results in part of the shadow "going missing"
What if the shadows aren't opaque?
If the object is convex, no problem: render the occluder using transparency. Use backface culling if two polygons are too many.
If not, then will have varying numbers of polygons at each pixel
Best solution: use the stencil buffer, allow only the first pixel of the occluder to be rendered
Why render the shadow every time? Wasteful if shadow don't move
Render the shadow into an offscreen texture that is rerendered only when
the shadow (light, occluder, receiver) changes
Make sure that the occluder is between the light and the receiver, else errors result

Can use the receiver to clip/cull potential occluders
What about receivers that aren't planes?
Shadow mapping (Williams 78)
Idea
Consider the scene from the view of the light source
What the light sees is not in shadow
How
Render the scene from the view of the light source
This creates depth values that can be located in 3D: the shadow map
When rendering the scene from the eye's viewpoint
Transform depths into the shadow map space
If depths are greater than those in the shadow map, corresponding object is in shadow
If in shadow, don't include light from this source

## Caveats

Have to render twice: once for light view, once for eye view
Can calculate depth only during light pass
Can reuse shadow map if light, occluder, receiver do not move (viewer can move)
Precision depends on $X Y$ and $Z$ resolution
Image aliasing
Problem
Resolution in light view is not resolution in eye view E.g. when a receiver is normal to one view, and orthogonal to other

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            E.g. fragments in eye will not generally match exactly to fragments in
                light view
Solutions
                            Can filter neighbors to get average (but this has its limits)
Depth aliasing
    Problem
        Can be hard to tell if an eye fragment is in front of a light fragment,
        especially if the views are not similar
    Solution
        Can add a "bias" constant to solve (works mostly, but not always)
            "Peter panning"
        Can change algorithm to use object IDs
            But then objects will never shadow themselves
    Flicker between frames
    Caused by changes in view sampling
    Can regenerate shadow map each frame, and use consistent sampling
    scheme
    Advantages
    Linear (2 passes)
    Works for arbitrary receivers
Shadow volumes
    Idea
        If the objects are polygonal, then so are the sides of the shadows
    We figure out what these sides are
    Then figure out if a fragment is inside the resulting volume
    How
    For each light
        For each edge in each polygon
            Define resulting shadow quadrilateral by
            Drawing ray from light to each vertex
        For each ray from the eye (for each eye fragment)
            Count the number of front facing sides it crosses f
            Count the number of backfacing sides it crosses b
            If f-b is positive, then fragment is in shadow
    Details
        For each light in each frame
            Clear stencil buffer
            Draw scene (without shadow volumes) using only ambient and emission,
            with z-buffering on
            Turn off frame and z-buffer updates (leave ztest on)
            Draw front facing shadow polygons
                Increment stencil for each fragment
            Draw backfacing shadow polygons
                Decrement stencil for each fragment
            Draw scene (without shadow volumes) using only diffuse and specular
                Apply diffuse and specular only if stencil value is zero
    Caveats
    Shadow pierces the front or back clipping planes
    Disadvantages
        Translucent objects
            As receiver: we only story the state of one object per pixel
            As occluder: we know only if we are in our out of shadow
        Slow
            Lots of fill processing in all the shadow polygons!
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